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Magneto-optical properties of InSb for terahertz applications

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Magneto-optical permittivity tensor spectra of undoped InSb, n-doped and p-doped InSb crystals were determined using the terahertz time-domain spectroscopy (THz-TDS) and the Fourier transform far-infrared spectroscopy (far-FTIR). A huge polar magneto-optical (MO) Kerr-effect (up to 20 degrees in rotation) and a simultaneous plasmonic behavior observed at low magnetic field (0.4 T) and room temperature are promising for terahertz nonreciprocal applications. We demonstrate the possibility of adjusting the spectral range with huge MO by increase in n-doping of InSb. Spectral response is modeled using generalized magneto-optical Drude-Lorentz theory, giving us precise values of free carrier mobility, density and effective mass consistent with electric Hall effect measurement. © 2016 Author(s). All article content, except where otherwise noted, is licensed under a Creative Commons Attribution (CC BY) license (<http://creativecommons.org/licenses/by/4.0/>). [<http://dx.doi.org/10.1063/1.4968178>]

Recent advances in the terahertz technology call for new devices and materials that would exhibit a non-reciprocal behavior in the terahertz range. One way to create the non-reciprocal behavior is the use of magneto-optical effects. Materials exhibiting a magneto-optical (MO) behavior at terahertz range are for example graphene,^{1,2} hexaferrites³ and semiconductors. General condition for successful applicability is the operation at low external magnetic field and at room temperature. Semiconductors are a viable choice, since their free carriers with low effective mass, either intrinsic or introduced by doping, allow for modulation of properties at these conditions.

The use of semiconductors in magneto-plasmonic devices for terahertz range has been suggested by Bolle et al.,⁴ while currently there are a number of studies, such as by Hu et al.,⁵ dealing with theoretical design of the devices. A correct implementation of the theoretical models is possible only when we know the exact properties of the materials used. Spectroscopic, non-destructive magneto-optical techniques give us the information we need.

The measurement of the free carrier magneto-optical effects in semiconductors has been called the “Optical Hall effect” by Kühne et al.² and Shubert et al.,⁶ who developed a far infrared and terahertz ellipsometric, full Mueller matrix method for semiconductor characterization. The potential of the terahertz time-domain spectroscopy (THz-TDS) in investigation of semiconductors had been recognized by Mittleman,⁷ (spatial inhomogeneities in GaAs), Jeon⁸ (reflectivity of GaAs and Si), Grishowski⁹ (properties Si, Ge, GaAs) and Ino¹⁰ (MO effect on InAs).

This letter deals with the magneto-plasmonic properties of InSb, since its low effective mass, $0.015 m_0$ at Γ point,¹¹ means its electrical and optical properties can be modulated by a small magnetic fields.

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The area of spectroscopy of InSb in magnetic field has been pioneered by Lax *et al.*,¹² while the subsequent theory had been summarized by Palik *et al.*^{13,14} and in references therein, who studied semiconductors with reflective, transmittance and coupled mode measurements in the far infrared range, at low temperatures (liquid helium or nitrogen) and very high fields (several Tesla). The works of Spitzer *et al.*¹⁵ combines reflectivity and electrical Hall effect characterization to derive effective mass/concentration data of n-doped InSb. The approach from microwave side of the spectrum has been established by Brodwin *et al.*¹⁶ and subsequently by Singh *et al.*,¹⁷ to characterize polycrystalline and single crystals of InSb at 9GHz, with temperature and magnetic field dependence. The findings have also been reviewed by Pidgeon¹⁸ and Kushwaha.¹⁹ Despite the wide range of semiconductors studied, the studies in the sixties and seventies were limited to the spectral range outside the terahertz gap (0.1-3 THz) due to a lack of available sources. Consequently, the authors had to use higher magnetic fields and low temperatures to observe interesting magneto-plasmonic effects in their spectral ranges, which is inconvenient for practical applications. Our aim is to show that InSb can be used as a magneto-plasmonic material in terahertz range at room temperature and using low external magnetic fields.

We measured four InSb crystals from the manufacturer MTI Corp, polished wafers of 2" diameter and 10×10 mm squares, $450 \mu\text{m}$ thick, undoped and with doping n (Te) and p (Ge). The n-doped squares sample and the wafer have different concentrations, denoted N_1 and N_2 respectively.

We used two spectrometers to characterize the samples. The first one is the terahertz time-domain spectrometer TPS Spectra 3000 from TeraView Co., measuring in the THz range of 2-100 cm^{-1} (0.06-3 THz). The beam was focused using parabolic mirrors, through wire-grid polarizer to the sample at near normal incidence and reflects back through the same polarizer, giving us polarized spectra of the sample. The terahertz spectrometer measures both the amplitude and the phase of the reflected wave. Measuring two correlated quantities and applying a model consistent with the Kramers-Kronig relations ensures a robust fit and data analysis.

The second one is the Fourier transform infrared spectrometer (FTIR) Bruker Vertex 70v, measuring in the far-infrared range of 50-680 cm^{-1} (1.5 - 20.4 THz), with the angle of incidence of 11 degrees and a variable analyzer and polarizer azimuths.

All measurements were done in vacuum, in reflection, with a thick gold layer as a reference. The reflectivity of all measured samples is in Figure 1, the data in overlapping ranges were averaged.

The plasma edges, noticeable as the minima in the reflectivity are indicators of the level of doping/intrinsic concentration. The concentrations of carriers in undoped and p-doped InSb are roughly the same, but the p-doped sample has a much shorter scattering time, hence the shallow shape of the plasma reflectivity. The phononic peak arising from the lattice vibrations is visible at around 179 cm^{-1} ; different positions observed in the reflectivity are due to the effect of the free carriers.

The measured data are fitted to the following model. The permittivity in the THz and the far-infrared range is described using the Drude-Lorentz model, a sum of three parts,

$$\epsilon_r = \epsilon_\infty - \underbrace{\frac{\omega_p^2}{\omega^2 + i\gamma_p\omega}}_{\epsilon_D} + \underbrace{\frac{A_L\omega_L^2}{\omega_L^2 - \omega^2 - i\gamma_L\omega}}_{\epsilon_L}, \quad (1)$$

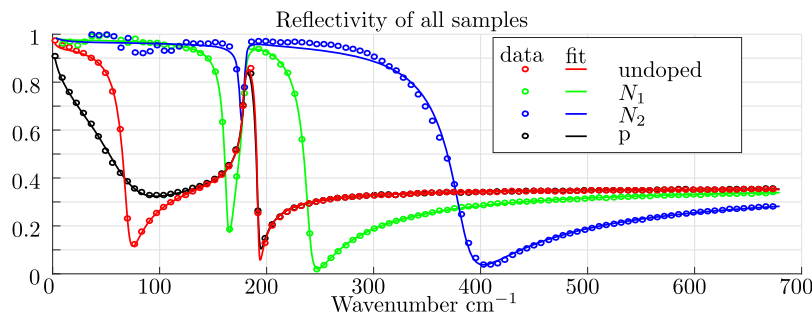


FIG. 1. Reflectivity of all InSb samples, TDS and FTIR data joined together.

where the constant term ε_∞ describes the background permittivity (high frequency absorptions), the Drude term ε_D describes the contribution of free carriers and the Lorentz term ε_L comes from the lattice vibrations. In the Drude term, the plasma frequency is defined as

$$\omega_p = \left(\frac{Ne^2}{\varepsilon_0 m^*} \right)^{\frac{1}{2}}, \quad (2)$$

where N is the carrier concentration, e is the electron charge, ε_0 is the permittivity of free space, $m^* = m_{\text{eff}} m_0$ is the effective mass of the charge carriers (m_0 is the mass of electron in vacuum) and $1/\gamma_p = \tau_p$ is the scattering time. The plasma frequency divided by $\sqrt{\varepsilon_\infty}$ is the frequency where the real part of permittivity crosses zero. The Lorentz term is characterized by the frequency ω_L , the scattering time $\tau_L = 1/\gamma_L$, and the amplitude A_L .

When an external magnetic field is applied, the Drude term becomes anisotropic. The TDS reflectivity and phase of the undoped InSb in the variable magnetic field are shown in Figure 2.

The reflectivity and phase of the samples is calculated using Berreman 4×4 method,²⁰ allowing for a full anisotropy modeling. Reflection is modeled as a single interface between vacuum and a semiconductor with the permittivity ε_r , along with Jones matrices to apply the effects of the used polarizers to the model.

The permittivity tensor used to describe the material with the magnetic field B applied in the z direction, perpendicular to the interface (MO polar configuration) is in the form

$$\hat{\varepsilon}_r = \begin{bmatrix} \varepsilon_{xx} & \varepsilon_{xy} & 0 \\ \varepsilon_{yx} & \varepsilon_{yy} & 0 \\ 0 & 0 & \varepsilon_{zz} \end{bmatrix}. \quad (3)$$

The ε_{zz} component stays the same as ε_r in (1) and xx , yy , xy , yx components change to

$$\varepsilon_{xx} = \varepsilon_{yy} = \varepsilon_\infty - \frac{\omega_p^2(\omega^2 + i\gamma_p\omega)}{(\omega^2 + i\gamma_p\omega)^2 - \omega_c^2\omega^2} + \varepsilon_L, \quad (4a)$$

$$\varepsilon_{xy} = -\varepsilon_{yx} = -i \frac{\omega_p^2\omega_c\omega}{(\omega^2 + i\gamma_p\omega)^2 - \omega_c^2\omega^2}, \quad (4b)$$

which contain an additional fitting parameter, proportional to the magnetic field, the cyclotron frequency, defined as

$$\omega_c = \frac{eB}{m^*}. \quad (5)$$

The Lorentz term can in theory be affected by the magnetic field, but the elements of the lattice are much heavier than electrons and the cyclotron frequency is negligible; the Lorentz term remains isotropic, as observed by Kühne at 8T in GaAs².

The phase information in Figure 2 comes from three parts, $\varphi = \varphi_{\text{sample}} - \varphi_{\text{reference}} - \varphi_{\text{shift}} \cdot \varphi_{\text{sample}}$ is the phase angle of the complex reflection coefficient of the sample and φ_{shift} stems from the

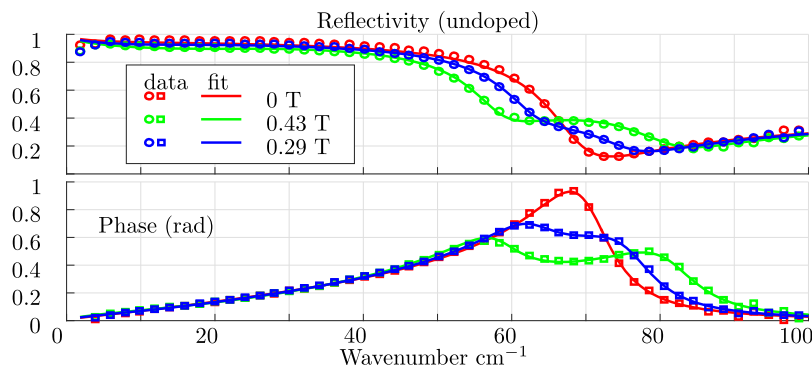


FIG. 2. TDS polarized reflectivity and corrected phase of undoped InSb in variable magnetic field.

misalignment d of the sample and reference, as $\varphi_{\text{shift}} = 4d\pi \cos \alpha_i / \lambda$. The φ_{shift} is a fitting parameter in the data treatment (d is on the order of 1-100 μm) and is subtracted from the data for plotting.

The magnetic field was created by a small permanent magnet with 0.43 T, with smaller fields obtainable through positioning of the magnet.

The measurements in different magnetic fields and no field were fitted together. The cyclotron frequency ω_c is 23.7 cm^{-1} for 0.43 T and the resulting effective mass of electrons in undoped InSb is $m_{\text{eff}} = (eB)/(\omega_c m_0) = 0.0169$, which in accordance to theory²¹ is higher than frequently used value of 0.015. The knowledge of both the cyclotron frequency and the plasma frequency allows also for the calculation of the carrier concentration and mobility $\mu = e\tau_p/m^*$ and is necessary for the correct theoretical prediction of the behavior of magneto-plasmonic devices.

The data from FTIR confirm the magneto-optical behavior of n-doped InSb, when the plasma frequency is pushed towards higher frequencies. Figure 3 shows the reflectivity of two n-doped samples when polarizer is at 45 degrees and analyzer at zero. When the direction of the magnetic field is reversed, the rotation of the reflected polarization changes direction, causing a drop/increase in reflected amplitude.

The parameters describing all samples are summarized in Table I. The non-magnetic properties of the undoped InSb match those reported or used by,^{5,22,23} but our measurements also allow for calculation of correct effective mass and concentration. The samples have also been measured electrically by the van der Pauw (VDP) method,²⁴ which is equivalent to $\omega \rightarrow 0$. The VDP data obtained are also listed in Table I and are reasonably close to those obtained by spectroscopic measurement. The n-doped samples exhibit lower cyclotron frequency at the same magnetic field, meaning that the effective mass is higher, which is again in agreement with the theory.²¹

Figure 4 show the obtained permittivity of all the samples using fitted parameters listed in Table I. The presence of a cyclotron frequency changes the low frequency limit of the real part of the diagonal components $\epsilon_{xx,yy}$, which can completely change sign, if the cyclotron frequency is high enough. The magnetic field also increases absorptions (Landau level absorption) at ω_c , noticeable mainly in the undoped InSb sample. This effect is usually observed when $\omega_c > \omega_p$ and also causes changes in the effective mass, which is negligible in our case due to low magnetic field.²⁵ The off-diagonal elements exhibit a peak around ω_c and a limit at low frequency (the classical Hall effect), while the imaginary part goes to infinity for low-frequencies.²⁶

Using the permittivity tensors we can further obtain the Kerr effect which is a good metric to describe the magneto-optical behavior of materials. The polar magneto-optical Kerr effect is a change of the polarization ellipse azimuth and ellipticity upon reflection of linearly polarized light from a sample in a magnetic field perpendicular to the interface.²⁷ Figure 5 shows the obtained rotation and ellipticity.

The Figures 4 and 5 give us the idea of the applicability of InSb as a magneto-plasmonic material. The magneto-optical effects is strongest around sharp changes in the original permittivity, either

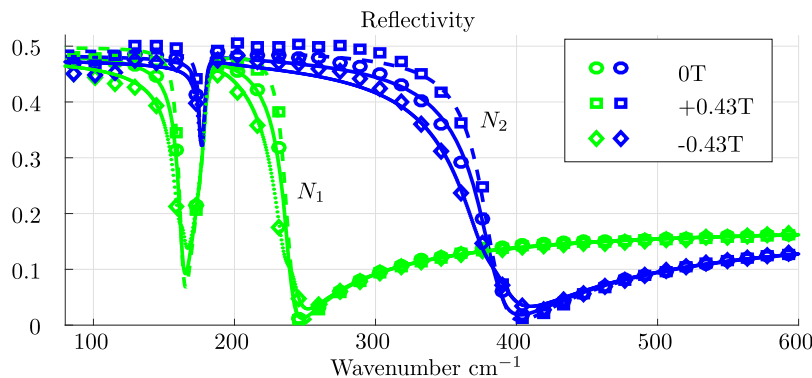


FIG. 3. Reflectivity of two concentrations of n-doped InSb, polarizer at 45. Data (symbols) and fit (curves) are compared. The center curve (circles, solid line) is reflectivity without the magnetic field, the other two are obtained for different signs of the magnetic field.

TABLE I. Fitted and calculated parameters of the samples.

Sample	$\omega_p/\sqrt{\epsilon_\infty}$ (cm^{-1})	τ_p 10^{-13} (s)	ω_L (cm^{-1})	τ_L 10^{-12} (s)	A_L	ω_c (cm^{-1})
und.	73.8 ± 0.1	5.53 ± 0.02	179.46 ± 0.05	2.00 ± 0.03	2.00 ± 0.01	23.76 ± 0.09
N_1	217.9 ± 0.2	4.00 ± 0.03	179.79 ± 0.03	1.66 ± 0.03	2.14 ± 0.01	11.25 ± 0.11
N_2	378.8 ± 0.3	2.01 ± 0.03	179.78 ± 0.03	1.74 ± 0.03	2.15 ± 0.01	13.99 ± 0.12
p	83.8 ± 0.3	0.75 ± 0.01	179.37 ± 0.05	1.89 ± 0.03	2.01 ± 0.01	
	ϵ_∞	m_{eff}	$N_{spec.}$ 10^{17} (cm^{-3})	$\mu_{spec.}$ 10^4 (cm/Vs)	N_{VDP} 10^{17} (cm^{-3})	μ_{VDP} 10^4 (cm^{-3})
und.	15.68 ± 0.03	0.0169 ± 0.0001	0.17 ± 0.008	5.76 ± 0.03	0.20	6.66
N_1	15.58 ± 0.02	0.0357 ± 0.0003	2.93 ± 0.003	1.97 ± 0.02	2.37	4.12
N_2	15.68 ± 0.02	0.0287 ± 0.0002	7.20 ± 0.006	1.23 ± 0.02	-	-
p	15.84 ± 0.02	-	-	-	10.7	0.02

around the plasma edge or the lattice vibration. There are regions, where the materials exhibit a strong Kerr rotation, a small Kerr ellipticity while the ϵ_{zz} component remains plasmonic, for undoped InSb its below 50 cm^{-1} (1.5 THz). For the n-doped samples, the behavior is similar, only shifted towards higher frequencies. This means that even though increasing carrier concentration increases effective mass and therefore lowers the cyclotron frequency, a strong magneto-plasmonic behavior

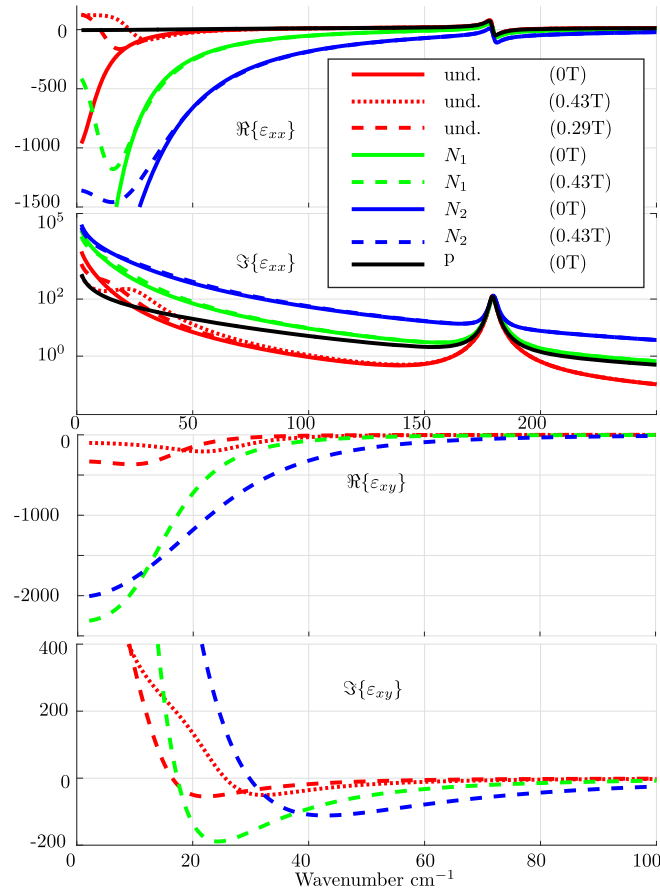
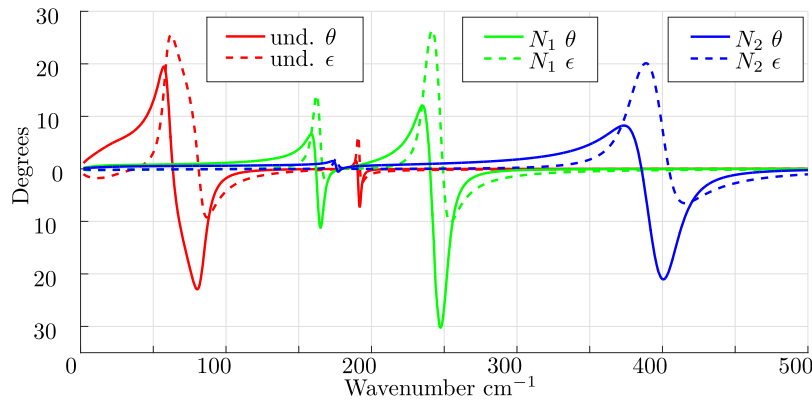


FIG. 4. Calculated diagonal and off-diagonal complex permittivity of all samples of InSb with and without applied magnetic field. Note the different ranges/scales to highlight important features.

FIG. 5. Obtained polar Kerr rotation θ and ellipticity ϵ .

is still present, allowing for a fine-tuning of the material and device properties. The p-doped sample didn't exhibit any measurable magneto-optical activity, due to very low cyclotron frequency caused by the effective mass of the heavy holes.

In conclusion, we have presented magneto-optical measurement of four samples of InSb with different carriers and carrier concentrations. The data are in good agreement with the Drude-Lorentz model in external magnetic field, both in the amplitude and phase, ensuring a valid use of the Kramers-Kronig relations. The materials exhibit a large magneto-plasmonic activity for the n-type carriers around the plasma edge, for all three levels of free electron concentration. The polar Kerr rotation is up to 20 degrees, which is higher than the data on InAs at 0.48 T by Shimano *et al.*,²⁸ which show Kerr rotation of 10 degrees around 1.5 THz. The strength of this effect at room temperature and reasonably low magnetic field points to applicability of InSb as a material for non-reciprocal magneto-plasmonic devices usable in the terahertz range, plus the properties can easily be further modulated by either heat²⁹ or light,²³ or the material can be used in a heterostructure in combination with different doping levels. The plasmonic properties can further enhance the magneto-optical effects by capturing, guiding and concentrating light at subwavelength scale using surface plasmons. Moreover, the physical properties obtained by spectroscopic measurement agree with electrical measurement and give us a correct value of the effective mass for further use in non-reciprocal device design.

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